



# An Optimization-based Multi-level Asset Allocation Model for Collaborative Planning

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- Introduction
- Mission scenario in MOC-2010 experiment
  - Force structure
  - Mission and task graph
- Collaborative planning module
  - Overall framework
  - Moving time horizon planning
  - Integrated (shared information) and isolated team structures
- Multi-level asset allocation problem
  - Problem description
  - Formulation
  - Solution approach
  - Algorithm performance
- Summary and future work

## ■ Motivation:

- Networked distributed planning capabilities in maritime operations centers (MOC)
- Mixed-initiative decision making
- Multi-level asset-to-task allocation
- Planning/re-planning based on dynamics of mission environment
- Assessing the efficiency and planning performance of integrated and isolated team structures (MOC-2010 experiment at NPS)

## ■ Previous research: optimization-based modules for MOC-2009 experiment

- Future operations (FOPS) module
  - Provide a list of  $N$ -best asset packages to maximize the task execution accuracy subject to constraints on maximum number of tasks per asset
- Current operations (COPS) module
  - Analysis the risk of redirecting assets from an ongoing task to perform intelligence, surveillance, and reconnaissance (ISR) tasks
- Scheduling (offline) module
  - Assist experimental designer to set the conditions for the mission planning activity (e.g., asset types and numbers, task requirements and asset capabilities)

**Q: Can we develop a general purpose distributed planning software for Team-in-the-loop planning experiments?**



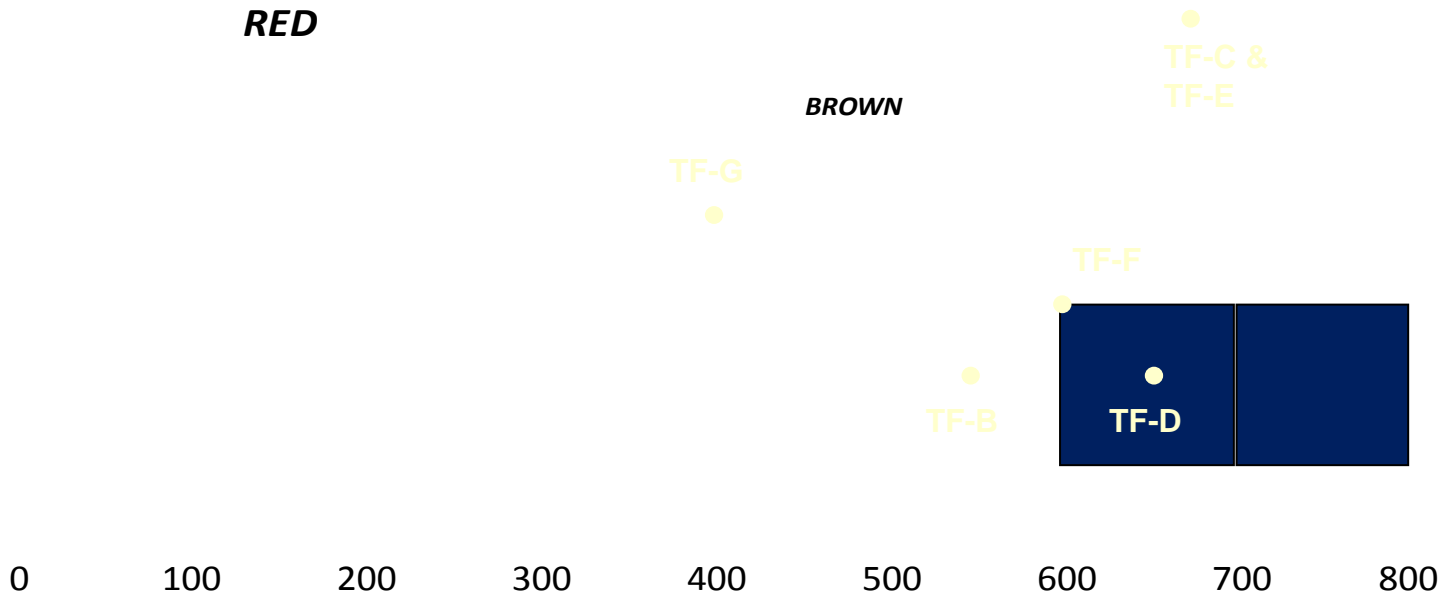
# Mission Scenario for MOC-2010 Experiment



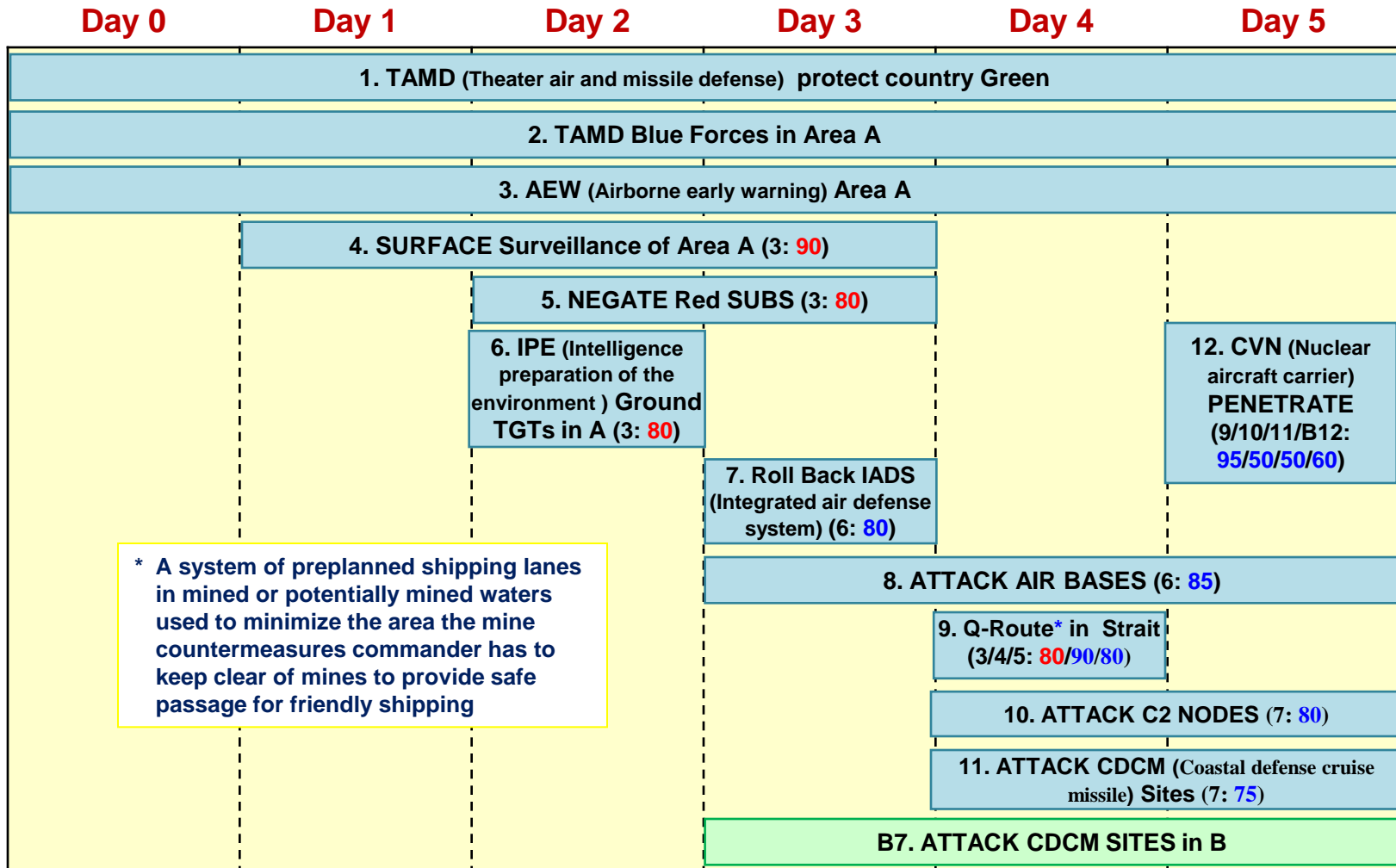
## Geographic Layout

600  
500  
400  
300  
200  
100  
0

Objective: Break area denial that has been established by Country Red as it tries to extend its influence over Country Brown by force.  
Secondary considerations: Allies in Country Green and own forces must be defended from any action by Red or Brown



## Task Graph (What needs to be done by what time?)



\* A system of preplanned shipping lanes in mined or potentially mined waters used to minimize the area the mine countermeasures commander has to keep clear of mines to provide safe passage for friendly shipping

- Similar mission courses of action (COA) exists for Area B
- Overall <15 Tasks per Day
- 25 Tasks of the mission

( ): Precedence task  
(task #: Accuracy or % Completion desired)

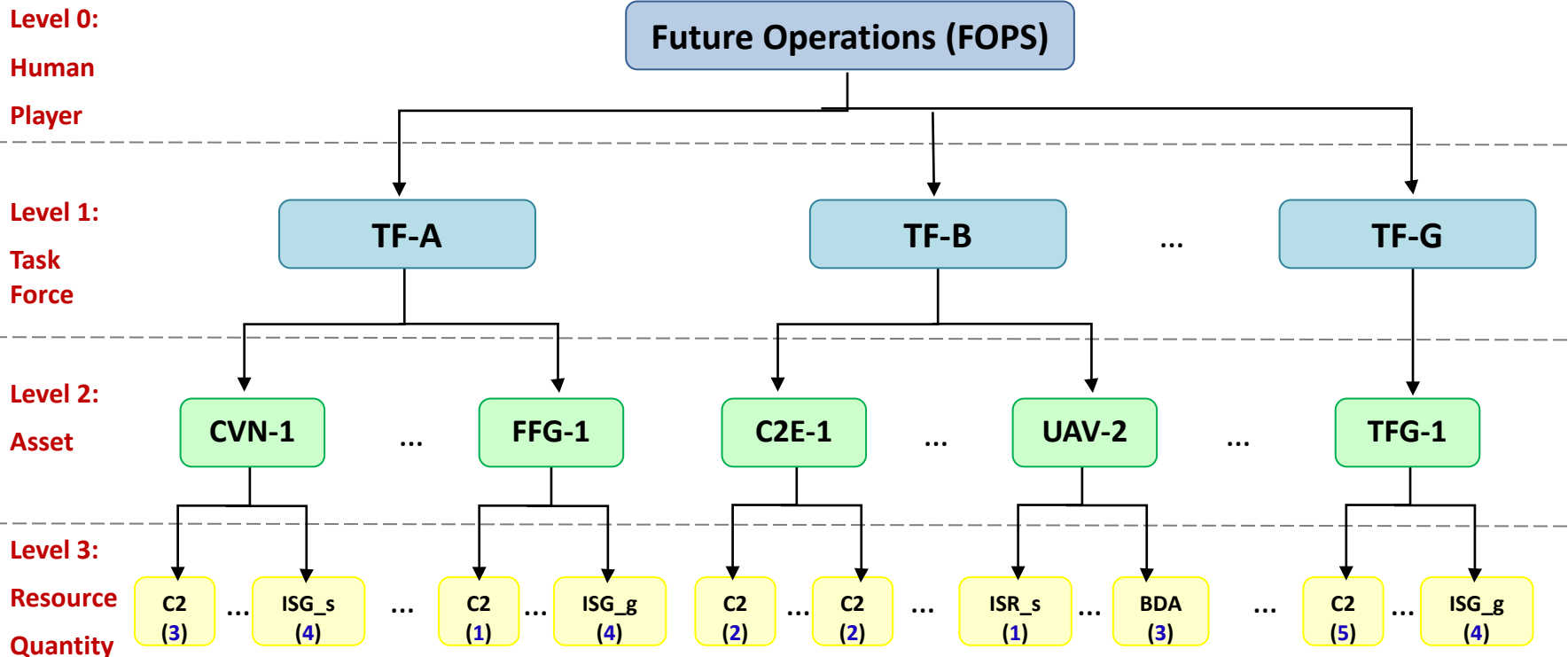
## ■ Planning Hierarchy (Specifies who does what and with which resources)

**4 FOPS at Level 0:** Assign Task Forces - Tasks with Supporting-Supported relationships with a desired performance criteria

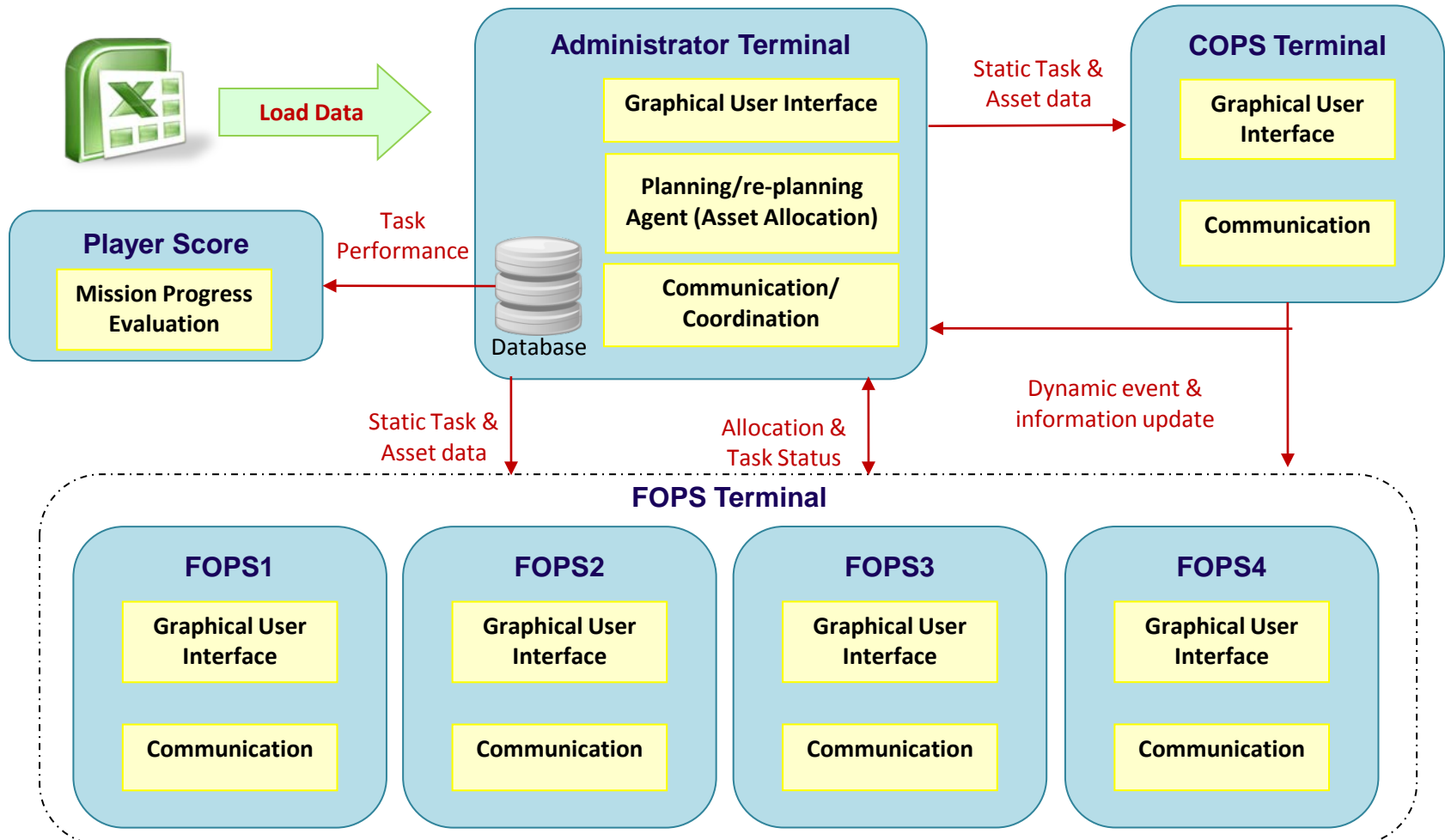
**7 Task Forces at Level 1:** an ESG, CSG, etc., specified with a geographical location

**42 Assets at Level 2:** specified with an arrival time to denote when the asset engaged to the mission

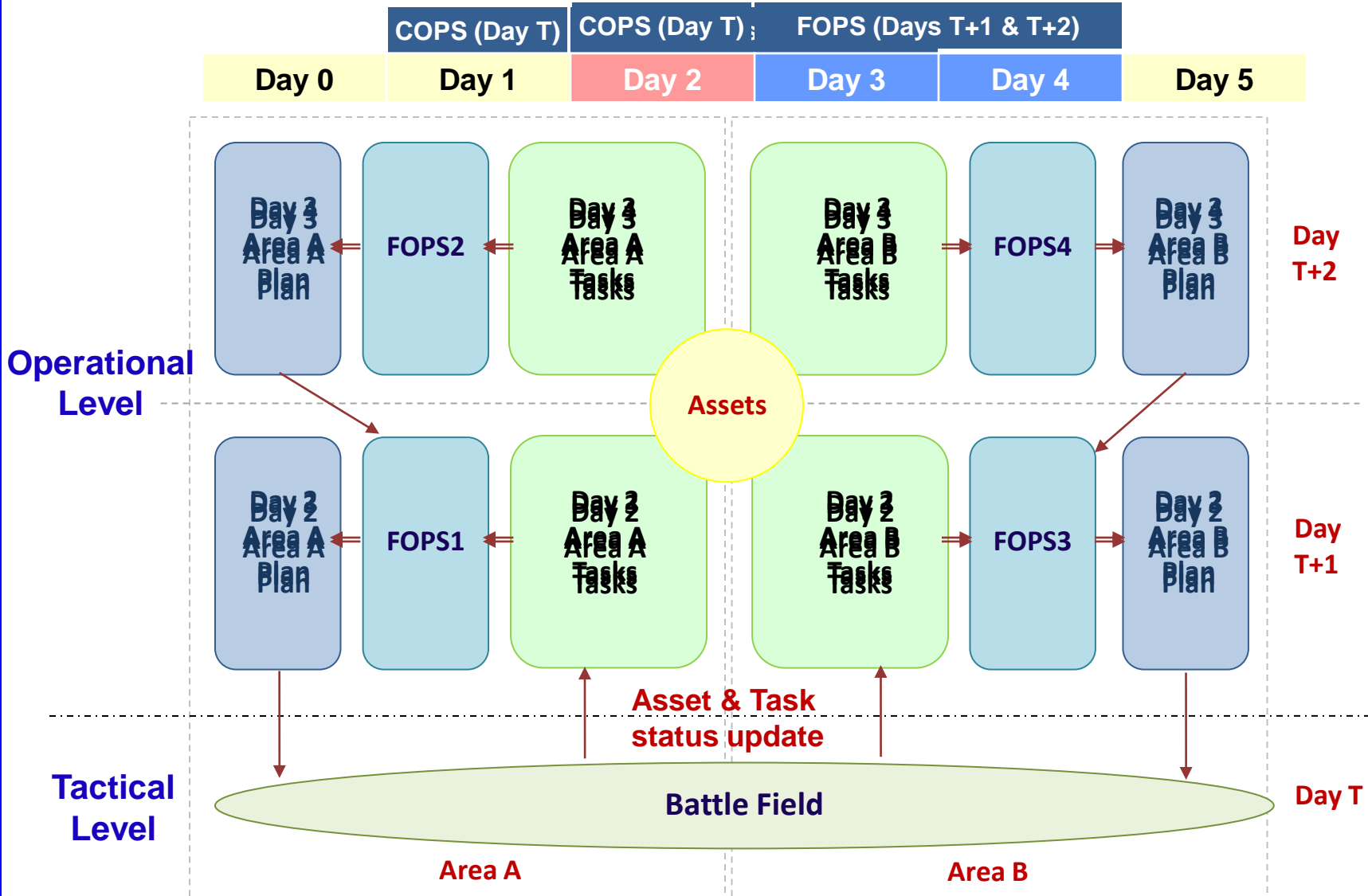
**331 Resource Quantities at level 3:** virtual entities with specified capabilities of each warfare area, e.g., C2, STRK, AW, etc.



- The planning module interacts with human players to
  - establish joint or individual commitments to tasks
  - monitor the execution of tasks and acknowledge the latest information
  - broadcast task performance and to re-plan the task

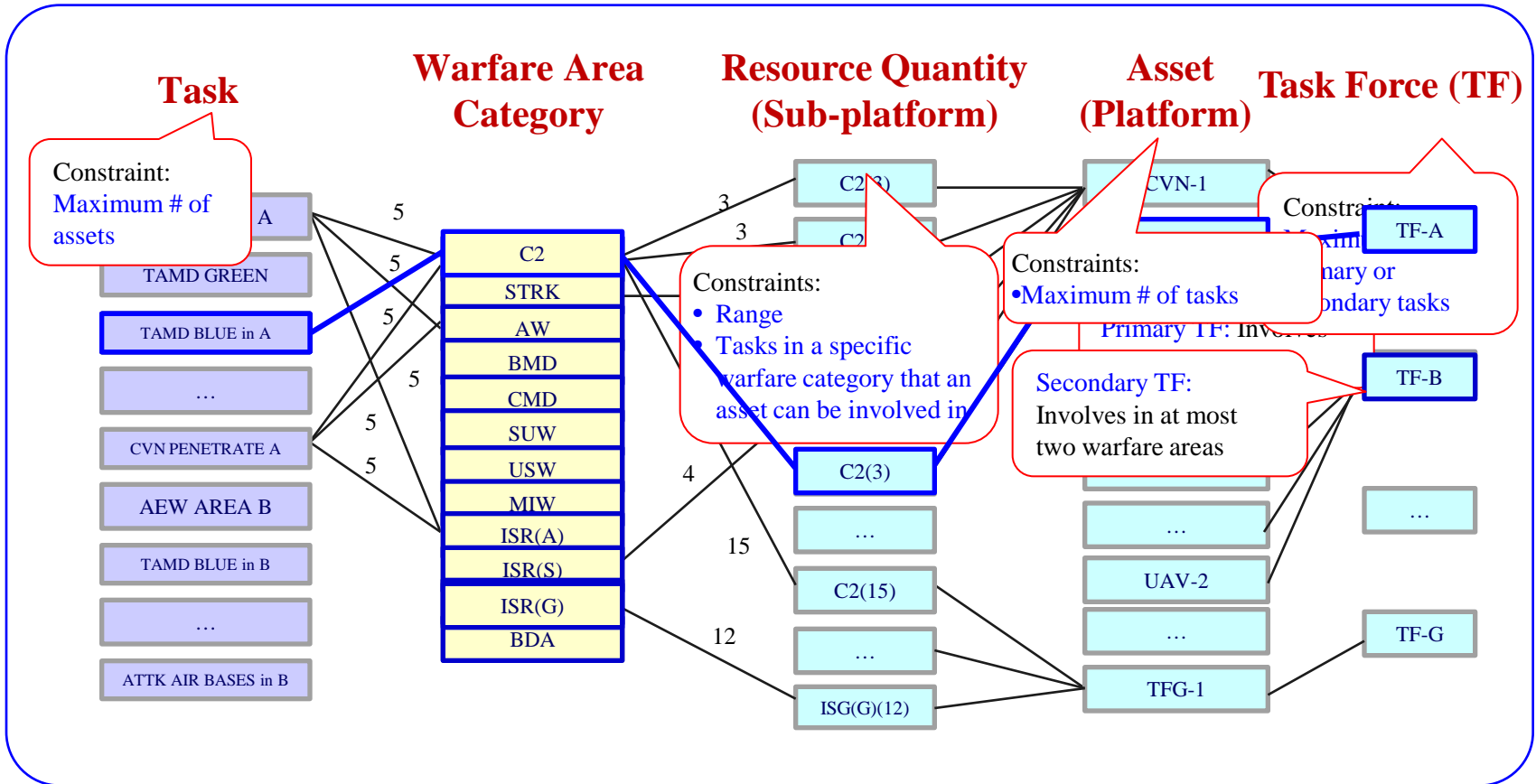


## ■ Moving Time Horizon Planning





- Problem Objective:** Minimize the cumulative difference between the **desired performance**(percentage completion/accuracy set by the human players) and the **expected performance**(generated by the planning agent based on allocation) over all the tasks



Decision variable: TF-Asset-Resource Quantity-Warfare Area-Task assignment array

$$\text{obj: } \min \sum_{i=1}^I \rho_i \frac{1}{M} \sum_{m=1}^M \left| \sum_{k \in \text{prmr}(i) \cup \text{scnd}(i)} \sum_{l=1}^{L(k)} \sum_{p=1}^{P(k,l,m)} \frac{\alpha_{klmp} z_{iklmp}}{R_{im}} - X_i \right|$$

... minimize the weighted tasks' deviation from the desired performances

$$\text{s.t } \frac{\sum_{p=1}^{P(k,l,m)} \alpha_{klmp} z_{iklmp}}{r_{klm}} \leq y_{iklm} \quad \forall i, k, l \text{ and } m$$

... assignment array between task and asset's specific warfare category

$$\sum_{m=1}^M y_{iklm} \leq M x_{ikl} \quad \forall i$$

... assignment array between task and asset

$$\sum_{k \in \text{prmr}(i) \cup \text{scnd}(i)} \sum_{l=1}^{L(k)} x_{ikl} \leq \text{max\_assets} \quad \forall i ;$$

...constraint on the maximal # of assets for a single task

$$\sum_{i=1}^I x_{ikl} \leq \text{max\_tasks} \quad \forall k \text{ and } l$$

...constraint on the maximal # of tasks for a single asset

$$\sum_{i=1}^I y_{iklm} \leq \text{max\_warfare\_tasks} \quad \forall k, l \text{ and } m;$$

... constraint on the maximal # of tasks for a single asset in specific warfare category

$$z_{iklmp} = 0 \quad \forall i, k \in \text{scnd}(i), 1 \leq l \leq L(k), m \in \phi(k,i), 1 \leq p \leq P(k,l,m)$$

... constraint on the secondary TF's supporting warfare categories

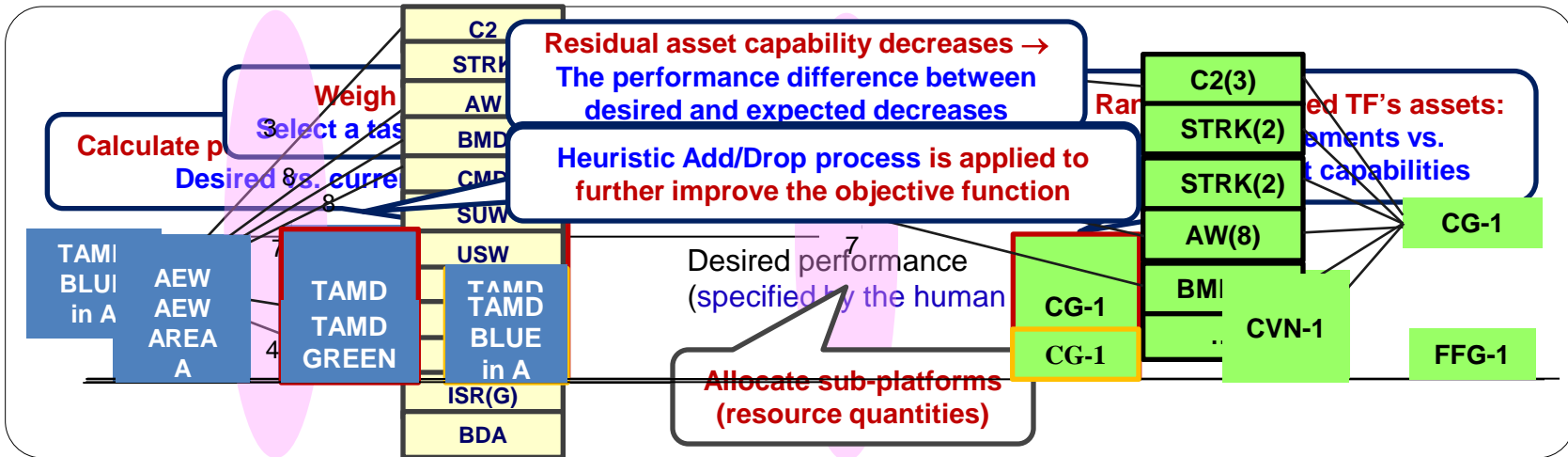
$$z_{iklmp} = 0 \quad \forall k, 1 \leq l \leq L(k), \forall m, 1 \leq p \leq P(k,l,m), i \in \zeta(k,m)$$

... geographic constraint ;

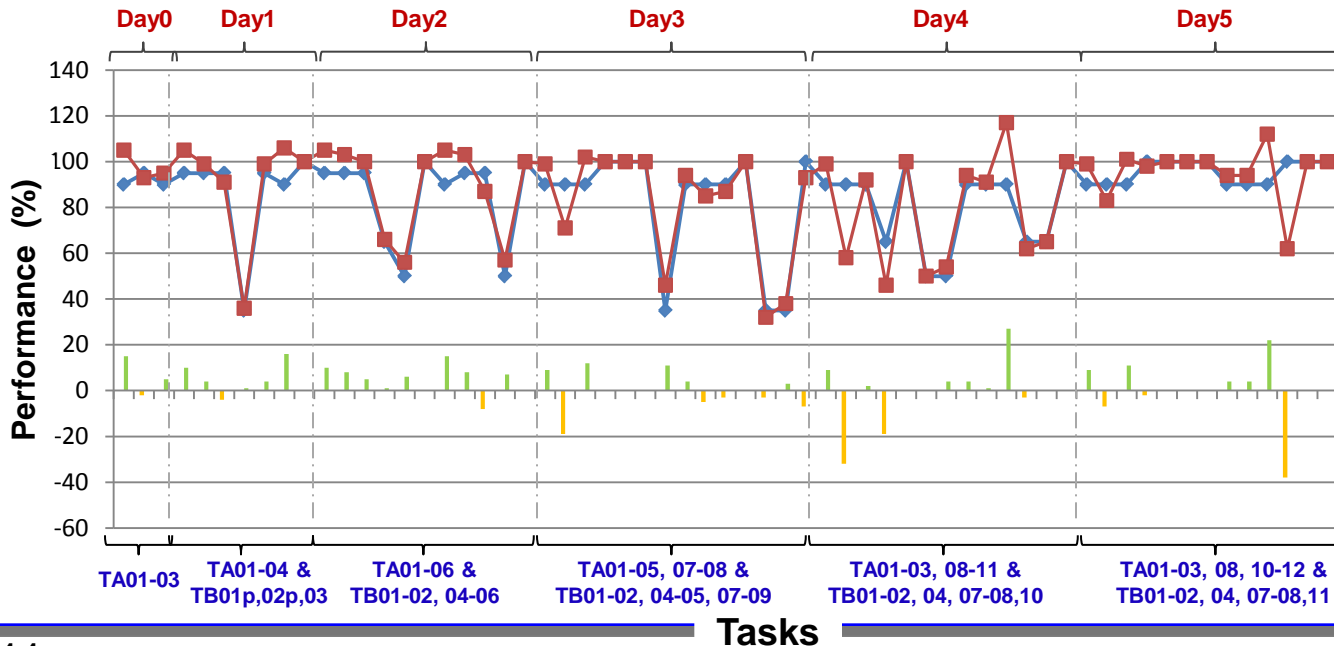
$$x_{ikl} \in (0,1), z_{iklmp} \in (0,1), y_{iklm} \in (0,1)$$

❖ Five Dimensional Assignment Array => 2000 decision variables per day  
❖ Complex constraints => 3000 constraints per day  
❖ Large scale Linear Integer Programming (LIP) Problem  
=> No polynomial run time solution

## Dynamic List Planning Method



## Desired vs. Expected Performance (Accuracy or % Completion)



- 61 tasks over 6 days: **<15/day**
- Average deviation from desired: **6.61%**
- Consistent primary TF allocation for the continuing tasks
- Run time: **< 10 sec / day vs. > 40 days** by exhaustive search



- **Summary: optimization-based multi-level asset allocation model**
  - Developed an interactive human-in-the-loop planning tool for **operational level planning among different team structures**
    - Mixed initiative human plus agent environment for laboratory research
  - The tool **accommodates the real world challenges** – information transfer, dynamic updates from the battlefield
  - Dynamic list planning method used to solve the **multi-level asset allocation** problem
- **Future research**
  - Integrate uncertainty factors in operational level planning
    - Weather impacts on planning included in MOC-2011 experiment
    - Uncertainty due to Logistics, ISR and weapon capabilities
  - Incorporate more realistic constraints
    - Temporal constraints: asset maintenance and refueling
    - Multi-level mission representations
  - Improve agent's capabilities
    - Develop operational level agents to optimize Task Force Assignment
    - Scheduling agents to determine optimized mission progress per day